

Some notes from class

2018-01-10

Definition

An axiomatic system is **consistent** if it is impossible to deduce from the axioms a theorem that contradicts any axiom or any theorem already proved from the axioms.

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Undefined terms: blip, trek Do those words apply here?

Axioms:

- 1 There are exactly five blips.
- 2 Every trek contains exactly two blips.
- 3 Every blip belongs to at most two treks.

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A little reminder about logic

Theorem

Let x and y be integers. Then x and y have the same parity if and only if $x + y$ is even.

How would we structure a proof of this?