

# Some notes from class

2018-01-16

# Logarithmic Differentiation

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$$g(x) = \frac{\ln x}{\ln 3} = \frac{1}{\ln 3} \ln x \quad \implies \quad g'(x) = \left( \frac{1}{\ln 3} \right) \frac{1}{x}$$