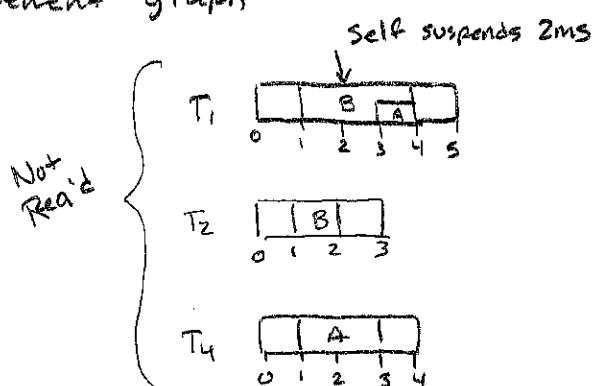
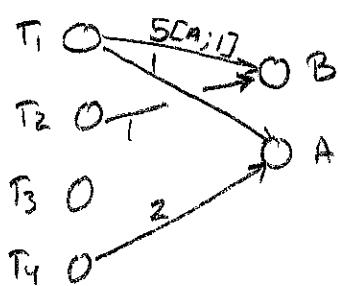


EE 4710 Study Guide

1. A system has 4 tasks $T_1 = (2, 12, 5; [B; 3[A; 1]])$

T_1 executes 1ms then takes B, executes 1 more 1ms then self-suspends 2ms. It then executes 1ms and takes A. after 1 more ms it releases A and B. Finally it executes 1 more ms and terminates. $T_2 = (3, 20, 3; [B; 1])$, $T_3 = (4, 25, 2)$ and $T_4 = (0, 30, 4; [A; 2])$. T_2 and T_4 execute 1ms before and after taking the resource.

a) Draw a resource requirement graph



b) Schedule these tasks using NPSCS protocol

T_4	T_4	T_1	T_1	T_1	T_1	T_2	T_2	T_2	T_2	T_3	T_3	T_4
0	1	2	3	4	5	6	7	8	9	10	11	12
T_4	A					B	AB	T_1	T_2	B	T_2	T_3

Should never self-suspend in non-preemptive critical section.

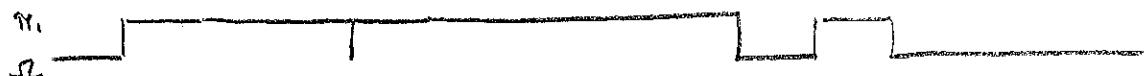
c) Schedule these tasks using Priority inheritance protocol

T_4	T_4	T_1	T_1	T_2	T_3	T_1	T_4	T_1	T_1	T_2	T_2	T_3	T_4
0	1	2	3	4	5	6	7	8	9	10	11	12	13
T_4	A					B	AB	T_1	T_2	B	T_2	T_3	T_4

T_2 cannot continue because T_4 promoted to T_1 .
 T_1 holds B

d) Schedule these tasks using the Priority Ceiling Protocol
 Also plot $\overline{\Pi}(t)$

T_4	T_4	T_1	T_4	T_1	T_2	T_3	T_1	T_1	T_2	T_2	T_3	T_4		
0	1	r_1	r_2	r_3	5	6	7	8	9	10	11	12	13	14



c) Schedule these tasks using ceiling priority protocol

$$\overline{\Pi}(A) = \overline{\Pi}_1 \quad \overline{\Pi}(B) = \overline{\Pi}_2$$

T_4	T_4	T_1	T_1	T_2	T_3	T_1	T_1	T_2	T_2	T_3	T_4	
0	1	r_1	r_2	r_3	5	7	8	9	10	12	13	14

T_4 running
at $\overline{\Pi}_1$

T_2 promoted
to $\overline{\Pi}_1$, must
wait for T_1 to
finish (FIFO)

T_2 returns
to $\overline{\Pi}_2$ but
still highest
priority

f) Can these tasks be scheduled using stack based PCP? Why.

A: No, Task 1 self suspends.

g) Assume Task 1 does not self-suspend. Schedule these tasks using stack based Priority ceiling Protocol, Plot $\overline{\Pi}(t)$

T_4	T_4	T_1	T_1	T_1	T_1	T_2	T_2	T_2	T_2	T_3	T_4			
0	1	r_1	r_2	r_3	4	5	6	7	8	10	11	12	13	14



Q. A system has 4 tasks. $T_1 = (15, 3; [X; 1])$, $T_2 = (25, 2)$,
 $T_3 = (30, 7; [X; 5[Y; 3]])$ and $T_4 = (50, 12; [Y; 3][X; 7])$

T_1 self suspends once for 1ms but not while X is held

T_2 self suspends twice for a total of 3ms

T_3 self suspends once for 1ms while holding X but not Y

- a) Find the blocking time due to self suspension $b_i(ss)$ for each task

$$x_1 = 1, x_2 = 3, x_3 = 1, x_4 = 0$$

$$b_1(ss) = x_1 = 1$$

$$b_2(ss) = x_2 + \min(x_1, e_1) = 3 + 1 = 4$$

$$b_3(ss) = x_3 + \min(x_1, e_1) + \min(x_2, e_2) = 1 + 1 + 2 = 4$$

$$b_4(ss) = x_4 + \min(x_1, e_1) + \min(x_2, e_2) + \min(x_3, e_3) = 0 + 1 + 2 + 1 = 4$$

- b) Suppose T_1 has a non-preemptive critical section of 0.5ms, T_2 has 2 sections of 0.3ms and 0.4ms. T_3 has a 0.2 ms critical section and T_4 has 3 critical sections 0.1 ms each. Find blocking time due to the worst case non-preemptive critical sections.

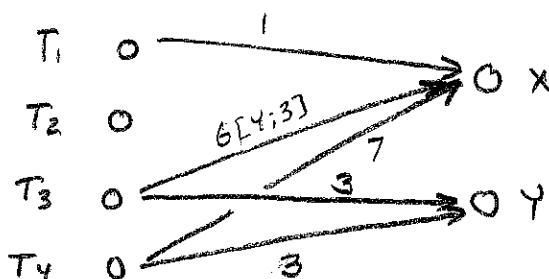
$$b_1(np) = \max(0.3, 0.4, 0.2, 0.1, 0.1, 0.1) = 0.4$$

$$b_2(np) = \max(0.2, 0.1, 0.1, 0.1) = 0.2$$

$$b_3(np) = \max(0.1, 0.1, 0.1) = 0.1$$

$$b_4(np) = 0$$

- c) Draw a resource requirement graph for this system



Remember T_3 self-suspends while holding X

d) Create direct and inheritance blocking tables for this system

	T ₂	T ₃	T ₄
T ₁	0	6	9
T ₂	-	0	0
T ₃	-	-	7



Note that for some protocols and this particular system, it would be impossible for T₁ to wait for both T₃ and T₄ because $\pi(X) = \pi(Y) = \pi_1$, but on the exam do not use that fact. Compute blocking times for the worst case.

	T ₂	T ₃	T ₄
T ₁	0	0	0
T ₂	-	5	9
T ₃	-	-	7

e) Find the blocking times $b_i(rc)$ due to resource contention

$$b_1(rc) = \max(5, 9) = 9$$

$$b_2(rc) = \max(5, 9) = 9$$

$$b_3(rc) = \max(7, 7) = 7$$

$$b_4(rc) = 0$$

f) Assume context switch time is 0.1 ms. Find the effective execution time for each task. Assume PCP.

of self suspensions: $k_1=1$, $k_2=2$, $k_3=1$

$$e_1 = 3 + 2(2+k_1)(0.1) = 3.6 \quad (\text{Takes a resource})$$

$$e_2 = 2 + 2(1+k_2)(0.1) = 2.6 \quad (\text{no resource})$$

$$e_3 = 7 + 2(2+k_3)(0.1) = 7.6$$

$$e_4 = 12$$

g) Find the total blocking time, b_i :

$$b_1 = b_1(ss) + (1+k_1)b_1(np) + b_1(rc) = 1 + 2(0.4) + 9 = 10.8$$

$$b_2 = b_2(ss) + (1+k_2)b_2(np) + b_2(rc) = 4 + 3(0.2) + 9 = 13.6$$

$$b_3 = b_3(ss) + (1+k_3)b_3(np) + b_3(rc) = 4 + 2(0.1) + 7 = 11.2$$

$$b_4 = b_4(ss) = 4$$

h) Find the time demand functions $w_i(t)$

$$w_1(t) = b_1 + e_1 = 10.8 + 3.6 = 14.4$$

$$\begin{aligned} w_2(t) &= b_2 + e_2 + \left\lceil \frac{t}{p_1} \right\rceil e_1 = 13.6 + 2.6 + \left\lceil \frac{t}{15} \right\rceil 3.6 \\ &= 16.2 + 3.6 \left\lceil \frac{t}{15} \right\rceil \end{aligned}$$

$$w_3(t) = 18.8 + 3.6 \left\lceil \frac{t}{15} \right\rceil + 2.6 \left\lceil \frac{t}{25} \right\rceil$$

$$w_4(t) = 16 + 3.6 \left\lceil \frac{t}{15} \right\rceil + 2.6 \left\lceil \frac{t}{25} \right\rceil + 7.6 \left\lceil \frac{t}{30} \right\rceil$$

i) Use time demand analysis to determine whether or not all deadlines can be met.

