

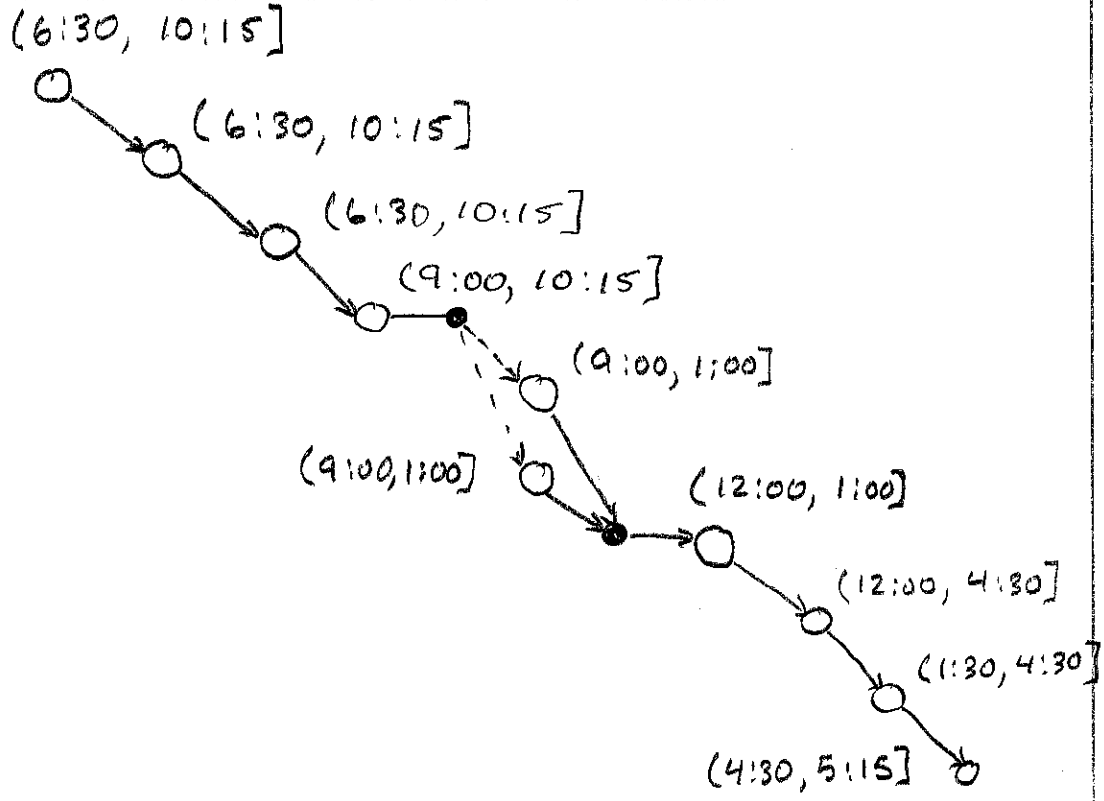
STUDY GUIDE

1. Draw a task graph and find feasible intervals for the tasks below. Assume Class is from 9:00-10:15, Lunch is served 12:00-1:00 and the afternoon bus leaves no earlier than 4:30 and arrives near your house no later than 5:15. Assume there are plenty of busses in the morning.

1. Wake up no earlier than 6:30 Am
 2. get ready
 3. ride bus to school
 4. catch at least a little of Dr. Brown's Class
- Either
5. Study, or
 6. Work on lab
- Then
7. Eat lunch
 8. Read
 9. Attend at least some of the 1:30-4:30 lab
 10. Ride the afternoon bus home

ANS

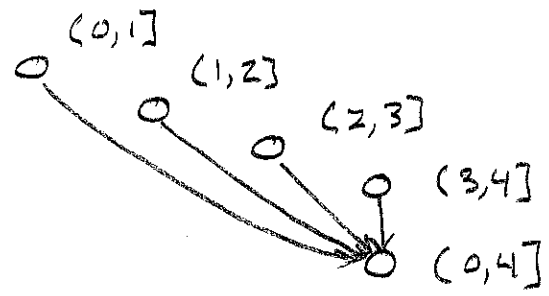
T₁
T₂
T₃
T₄
T₅
T₆
T₇
T₈
T₉
T₁₀



2. A certain scale uses a single A/D converter to read 4 load cells and a calibration reference. All 4 measurements are required to compute a weight. J₁, J₂, J₃ and J₄ read the 4 inputs, J₅ computes the weight. The A/D can only be started in integer intervals (i.e. (0,1], (1,2] etc.) All jobs have a period of 4, but $\phi_1=0$, $\phi_2=1$, $\phi_3=2$ and $\phi_4=3$. Also $D_1=D_2=D_3=D_4=1$. Draw a task graph. Ignore control dependencies. Show feasible intervals.

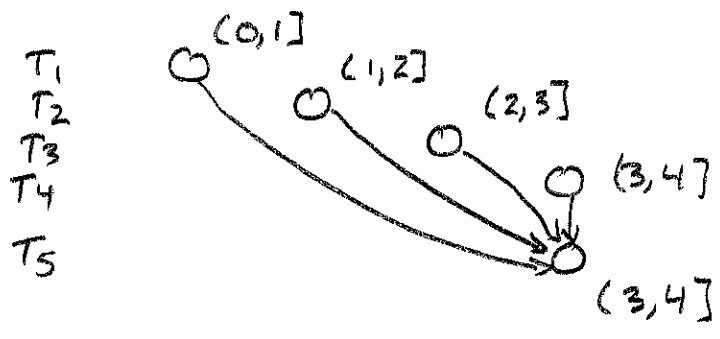
ANS

T₁
T₂
T₃
T₄
T₅

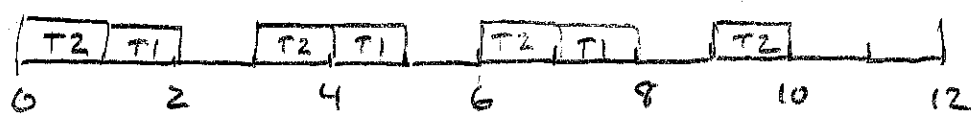


3. Draw another task graph, but show effective release times and deadlines.

ANS



4. Consider $T_1 = (4, 1)$, $T_2 = (3, 1)$. Is the schedule below valid? Explain.



ANS

No, Either T_1 starts at 7 before it is released at 8, or it has been given too much time in interval $(4, 8]$.

5. Is the schedule in 4 feasible? Explain.

ANS

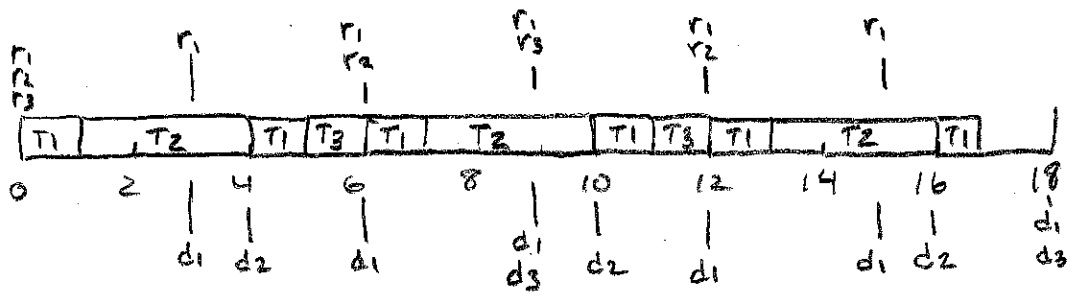
No, A feasible schedule must also be valid.

6. Schedule the following tasks for a clock-driven scheduler using EDF.

$T_1 = (3, 1)$, $T_2 = (6, 3, 4)$, $T_3 = (9, 1)$

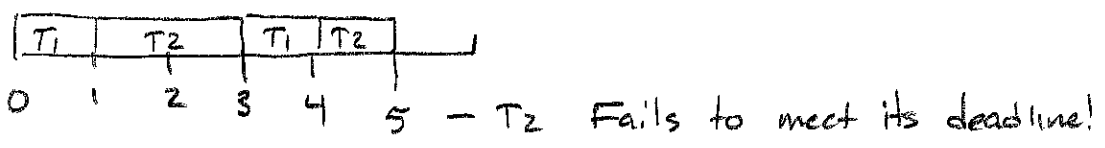
$H = \text{LCM}(3, 6, 9) = 18$

ANS



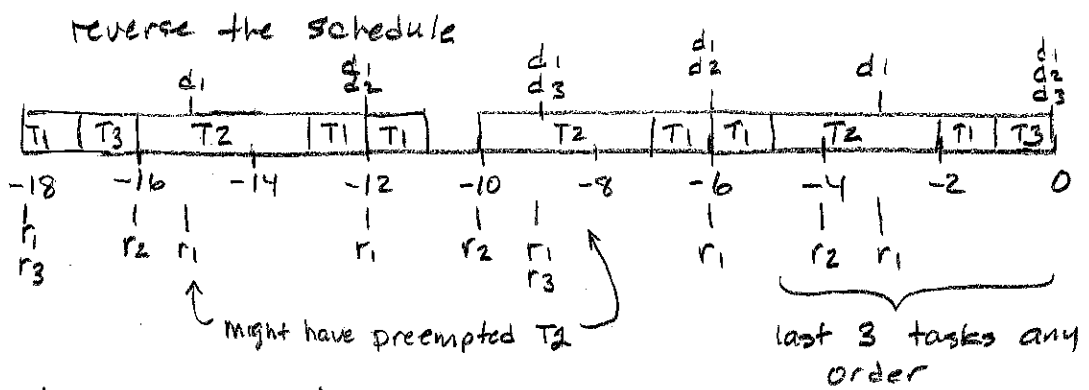
7. If the Tasks in problem 6 are scheduled with the DM algorithm. Will it meet its deadlines (solve by attempting to schedule the critical instant for all tasks)

ANS

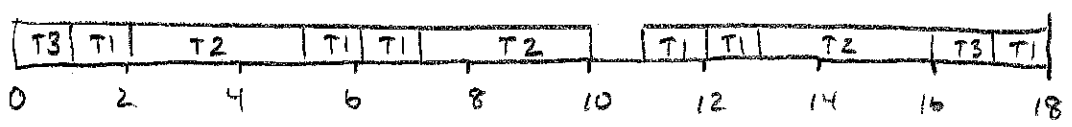


8. Schedule the tasks in problem 6 using LRT

ANS



Now, reverse it back:



9. Find the candidate frame sizes for the tasks $(3, 1.2)$, $(4, 0.8)$, $(6, 0.6)$, $(6, 0.3)$

ANS

1. $f \geq 1.2$

2a. $f \leq \min(p_i) = 3$

b. $nf = H = 12$, $f = 3, \frac{12}{5}, 2, \frac{12}{7}, \frac{3}{2}, \frac{4}{3}, \frac{6}{5}$

3. $2f \leq D_i + \gcd(f, p_i) \quad \forall i$

Clearly $f \leq \frac{3}{2}$ are candidates because $\min(D_i) = 3$

But now we must check $f=3, \frac{12}{5}, 2$ and $\frac{12}{7}$ manually

$$\text{Try } f=3: \quad 2(3) \stackrel{?}{\leq} 3 + \gcd(3, 3) = 6 \quad \checkmark$$

$$2(3) \stackrel{?}{\leq} 4 + \gcd(3, 4) = 5 \quad \times$$

$$\text{Try } f=\frac{12}{5}: \quad 2\left(\frac{12}{5}\right) \stackrel{?}{\leq} 3 + \gcd\left(\frac{12}{5}, 3\right) = 3\frac{3}{5} \quad \times$$

$$\text{Try } f=2: \quad 2(2) \stackrel{?}{\leq} 3 + \gcd(2, 3) = 4 \quad \checkmark$$

$$2(2) \stackrel{?}{\leq} 4 + \dots \quad \checkmark$$

obvious for $p_i = 6$

$$\text{Try } f=\frac{12}{7}: \quad 2\left(\frac{12}{7}\right) \leq 3 + \gcd\left(\frac{12}{7}, 3\right) = 3\frac{3}{7} \quad \checkmark$$

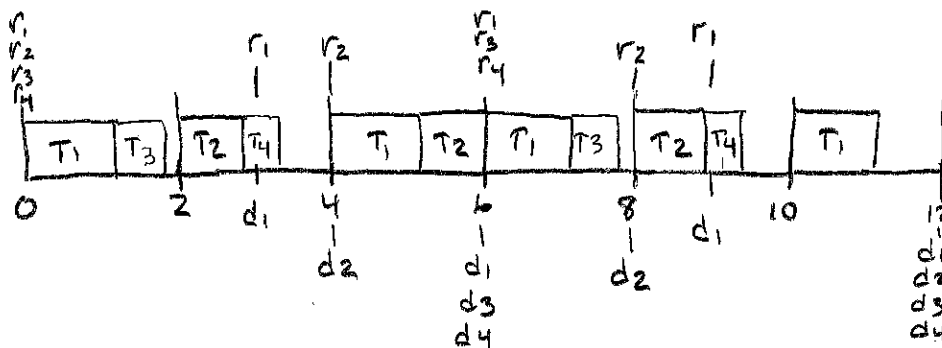
$$2\left(\frac{12}{7}\right) \leq 4 + \dots \quad \checkmark$$

obvious for $p_i = 6$

So candidates are $\boxed{2, \frac{12}{7}, \frac{3}{2}, \frac{4}{3}, \frac{6}{5}}$

10. Suppose you choose a frame size of 2 in problem 9. Can the tasks be scheduled? if so, give the schedule. If not, Explain.

ANS



This is one possible schedule, there are others.

11. Suppose The tasks in Problem 9 can be Scheduled, and that 2 aperiodic tasks run in the background. Assume the first has an execution time uniformly distributed between 1 and 2, and the second has an execution time of 1, 90% of the time and 2 10% of the time. The first has an average interarrival period of 50 and the second has an average interarrival period of 25

a) find the utilization, u , due to periodic tasks.

ANS
$$u = \frac{1.2}{3} + \frac{0.8}{4} + \frac{0.6}{6} + \frac{0.3}{6} = \boxed{0.75}$$

b) find the utilization, u_A , of the aperiodic tasks:

ANS
$$u_A = \sum \lambda_i E[\beta_i]$$

$$E[\beta_1] = 1.5, \quad E[\beta_2] = (1)(0.9) + (2)(0.1) = 1.1$$

$$\lambda_1 = \frac{1}{50} = 0.02, \quad \lambda_2 = \frac{1}{25} = 0.04$$

$$(0.02)(1.5) + (0.04)(1.1) = 0.03 + 0.044 = \boxed{0.074}$$

c) Find the average response time of the aperiodic tasks

ANS
$$W = \frac{u_A}{\lambda(1-u)} + \frac{W_0}{(1-u)^2 \left[1 - \left(\frac{u_A}{1-u}\right)\right]}$$

$$\text{But } w_0 = \frac{1}{2} \sum_i \lambda_i E[B_i^2]$$

$$E(B_1^2) = \int_1^2 x^2 dx = \left. \frac{x^3}{3} \right|_1^2 = \frac{8}{3} - \frac{1}{3} = \frac{7}{3}$$

$$E(B_2^2) = (1^2)(0.9) + (2^2)(0.1) = 1.3$$

$$w_0 = \frac{1}{2} (0.02 \left(\frac{7}{3}\right) + 0.04(1.3)) = 0.052\bar{6}$$

$$\lambda = \lambda_1 + \lambda_2 = 0.02 + 0.04 = 0.06$$

Finally

$$w = \frac{0.074}{(0.06)(1-0.75)} + \frac{0.052\bar{6}}{(1-0.75)^2 \left[1 - \frac{0.074}{1-0.75}\right]}$$

$$= 4.9\bar{3} + 1.197 = \boxed{6.13}$$

12. State whether or not the following tasks can be scheduled with (a) EDF, and (b) DM

a) $T_1 = (3, 1, 2)$, $(10, 2.5)$ and $(21, 1, 20)$

ANS $\Delta_1 = \frac{1}{2}$, $\Delta_2 = \frac{1}{4}$, $\Delta_3 = \frac{1}{4}$, so they are schedulable under EDF.

For DM, accelerated schedule is simple periodic, so $U = 1.0$, but that is sufficient to prove schedulable.

b) $T_1 = (6, 2)$, $T_2 = (11, 4)$, $T_3 = (14, 3)$,
 $T_4 = (19, 2)$.

ANS Utilization is $u = 1.017$. No scheduling algorithm will schedule these tasks.

c) $T_1 = (9, 3)$, $T_2 = (11, 5)$

ANS $u = 0.788 \leq 1$ so schedulable under EDF.

In this case $DM = RM$, so

$$u \stackrel{?}{\leq} n(2^{1/n} - 1) = 0.828$$

$0.788 < 0.828$, so schedulable under DM.

d) $T_1 = (3, 1)$, $T_2 = (4, 1)$, $T_3 = (8, 2, 7)$

ANS $\Delta = 0.869 \leq 1$ so schedulable under EDF.

For accelerated schedule, $u = 0.869$

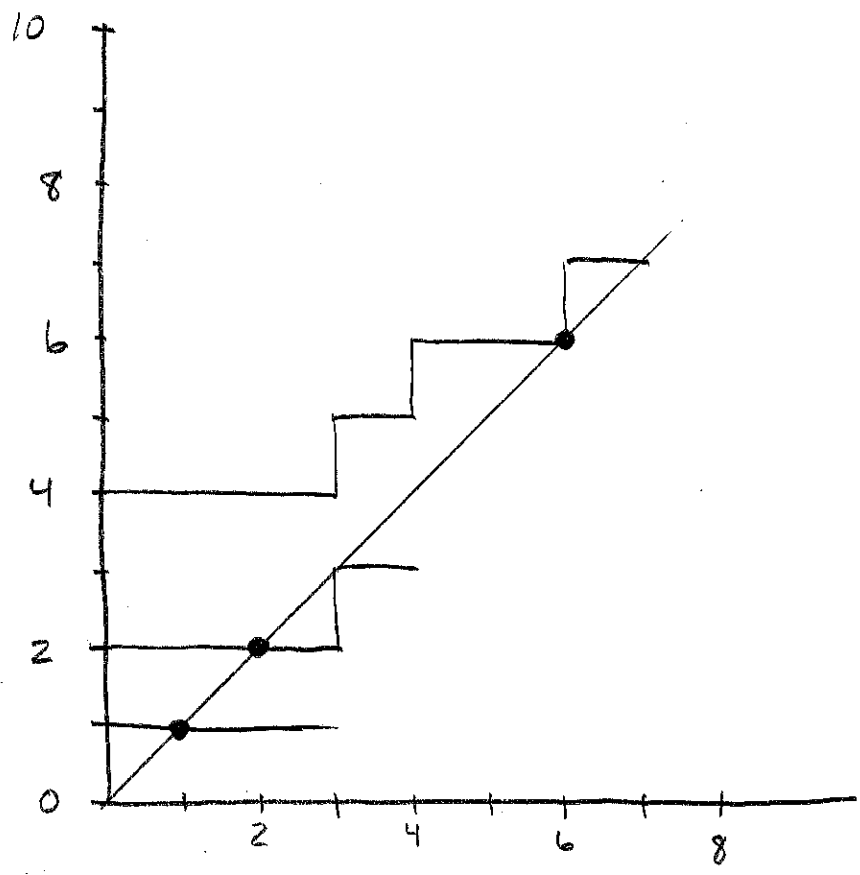
$$0.869 \stackrel{?}{\leq} n(2^{1/n} - 1) = 3(2^{1/3} - 1) = 0.778$$

We cannot tell if these tasks are schedulable under DM using this method, so we use time Demand Analysis.

$$w_1(t) = 1$$

$$w_2(t) = 1 + \left\lceil \frac{t}{3} \right\rceil$$

$$w_3(t) = 2 + \left\lceil \frac{t}{3} \right\rceil + \left\lceil \frac{t}{4} \right\rceil$$



These tasks are schedulable under DM.